

(See <https://cs.stanford.edu/~knuth/programs.html> for date.)

1. Intro. Sequence M1805, posets with linear order $1 \dots n$. Same as upper triangular $n \times n$ Boolean matrices B with zeros on diagonal and $B^2 \subseteq B$.

The unique(?) thing here is that I use 2^k as an index, not k ; therefore I can also use $2^k + 2^l$ as an index into a triangular matrix!

```

#define maxn 9
#define maxnn (1 << (maxn - 1))
#include <stdio.h>
int row[maxnn + 1]; /* row[1 << (n - j)] is jth row of B */
int mask[maxnn + (maxnn >> 1) + 1];
/* mask[1 << (n - j)] shows bits that must be zero in jth row */
int sols;
main()
{
  register int l, x, y, z;
  int n, nn;
  for (n = 3; n ≤ maxn; n++) {
    sols = 0;
    l = nn = 1 << (n - 1);
    for (x = 2; x ≤ l; x <<= 1) mask[x] = 0;
  newlev: if (l ≡ 2) {
    sols += 2 - (mask[2] & 1);
    goto backtrack;
  }
  mask[l] &= l - 1;
  row[l] = 0;
  l >>= 1;
  goto newlev;
  backtrack: l <<= 1, x = row[l];
  for (y = x & (x + 1); y; y -= z) z = y & -y, mask[z] = mask[l + z];
  x = (x | mask[l]) + 1;
  if (x ≥ l) {
    if (l ≡ nn) goto done;
    goto backtrack;
  }
  row[l] = x = x & ~mask[l];
  for (y = x & (x + 1), x = x ⊕ -1; y; y -= z) z = y & -y, mask[l + z] = mask[z], mask[z] |= x;
  l >>= 1;
  goto newlev;
  done: printf("%d solutions for %d.\n", sols, n);
}
}

```

2. Index.

backtrack: [1](#).

done: [1](#).

l: [1](#).

main: [1](#).

mask: [1](#).

maxn: [1](#).

maxnn: [1](#).

n: [1](#).

newlev: [1](#).

nn: [1](#).

printf: [1](#).

row: [1](#).

sols: [1](#).

x: [1](#).

y: [1](#).

z: [1](#).

POSETS0

	Section	Page
Intro	1	1
Index	2	2