

(See <https://cs.stanford.edu/~knuth/programs.html> for date.)

**1. Data for dancing.** This program creates data suitable for the DANCE routine, given the description of a board to be covered and a set of polyiamond shapes.

The first line of input names all the board positions, in any order. Each position is a two-digit number representing  $x$  and  $y$  coordinates, or a two-digit number followed by an asterisk; each “digit” is a single character, 0–9 or a–z representing the numbers 0–35. The asterisk denotes a triangle with point down. For example,

00 00\* 01 10

is one way to describe a triangular board, two units on a side.

The second line of input names all the pieces. Each piece name consists of at most three characters; the name should also be distinguishable from a board position. (The program does not check this.)

The remaining lines of input describe the polyiamonds. First comes the name, followed by two integers  $s$  and  $t$ , meaning that the shape should appear in  $s$  rotations and  $t$  transpositions. Then come two-digit coordinates for each cell of the shape. For example, the line

G 6 2 00\* 01 01\* 10 10\* 20

describes a hexiamond that can appear in 12 orientations. (See the analogous program for polyominoes.)

```
#define max_pieces 100 /* at most this many shapes */
#define buf_size 36 * 36 * 3 + 8 /* upper bound on line length */

#include <stdio.h>
#include <ctype.h>
    ⟨ Global variables 4 ⟩
    ⟨ Subroutines 3 ⟩;

main()
{
    register char *p, *q;
    register int j, k, n, x, y, z;
    ⟨ Read and output the board 2 ⟩;
    ⟨ Read and output the piece names 5 ⟩;
    ⟨ Read and output the pieces 6 ⟩;
}
```

2. `#define panic(m)`  
`{ fprintf(stderr, "%s!\n%s", m, buf); exit(-1); }`

`< Read and output the board 2 > ≡`

```

fgets(buf, buf_size, stdin);
if (buf[strlen(buf) - 1] ≠ '\n') panic("Input_line_too_long");
bxmin = bymin = 35; bxmax = bymax = 0;
for (p = buf; *p; p += 3) {
    while (isspace(*p)) p++;
    if (!*p) break;
    x = decode(*p);
    if (x < 0) panic("Bad_x_coordinate");
    y = decode(*(p + 1));
    if (y < 0) panic("Bad_y_coordinate");
    if (*(p + 2) == '*') p++, z = 1; else z = 0;
    if (!isspace(*(p + 2))) panic("Bad_board_position");
    if (board[x][y][z]) panic("Duplicate_board_position");
    if (x < bxmin) bxmin = x;
    if (x > bxmax) bxmax = x;
    if (y < bymin) bymin = y;
    if (y > bymax) bymax = y;
    board[x][y][z] = 1;
}
if (bxmin > bxmax) panic("Empty_board");
fwrite(buf, 1, strlen(buf) - 1, stdout); /* output all but the newline */

```

This code is used in section 1.

3. `< Subroutines 3 > ≡`

```

int decode(c)
char c;
{
    if (c ≤ '9') {
        if (c ≥ '0') return c - '0';
    } else if (c ≥ 'a') {
        if (c ≤ 'z') return c + 10 - 'a';
    }
    return -1;
}

```

See also section 12.

This code is used in section 1.

4. `< Global variables 4 > ≡`

```

char buf[buf_size];
int board[36][36][2]; /* cells present */
int bxmin, bxmax, bymin, bymax; /* used portion of the board */

```

See also section 7.

This code is used in section 1.

5. `< Read and output the piece names 5 > ≡`

```

if (!fgets(buf, buf_size, stdin)) panic("No_piece_names");
printf("\n%s", buf); /* just pass the piece names through */

```

This code is used in section 1.

6.  $\langle$  Read and output the pieces 6  $\rangle \equiv$

```

while (fgets(buf, buf_size, stdin)) {
    if (buf[strlen(buf) - 1] ≠ '\n') panic("Input_line_too_long");
    for (p = buf; isspace(*p); p++) ;
    if ( $\neg *p$ ) panic("Empty_line");
    for (q = p + 1; !isspace(*q); q++) ;
    if (q > p + 3) panic("Piece_name_too_long");
    for (q = name; !isspace(*p); p++, q++) *q = *p;
    *q = '\0';
    for (p++; isspace(*p); p++) ;
    s = *p - '0';
    if ((s ≠ 1 ∧ s ≠ 2 ∧ s ≠ 3 ∧ s ≠ 6)  $\vee \neg \text{isspace}(*(\text{p} + 1))$ ) panic("Bad_s_value");
    for (p += 2; isspace(*p); p++) ;
    t = *p - '0';
    if ((t ≠ 1 ∧ t ≠ 2)  $\vee \neg \text{isspace}(*(\text{p} + 1))$ ) panic("Bad_t_value");
    n = 0;
    xmin = ymin = 35; xmax = ymax = 0;
    for (p += 2; *p; p += 3, n++) {
        while (isspace(*p)) p++;
        if ( $\neg *p$ ) break;
        x = decode(*p);
        if (x < 0) panic("Bad_x_coordinate");
        y = decode(*(\text{p} + 1));
        if (y < 0) panic("Bad_y_coordinate");
        if ( $\ast(\text{p} + 2) \equiv '*'$ ) p++, z = 1; else z = 0;
        if ( $\neg \text{isspace}(*(\text{p} + 2))$ ) panic("Bad_board_position");
        if (n ≡ 36 * 36 * 2) panic("Pigeonhole_principle_says_you_repeated_a_position");
        xx[n] = x, yy[n] = y, zz[n] = z;
        if (x < xmin) xmin = x;
        if (x > xmax) xmax = x;
        if (y < ymin) ymin = y;
        if (y > ymax) ymax = y;
    }
    if (n ≡ 0) panic("Empty_piece");
     $\langle$  Generate the possible piece placements 8  $\rangle$ ;
}

```

This code is used in section 1.

7.  $\langle$  Global variables 4  $\rangle +\equiv$

```

char name[4]; /* name of current piece */
int s, t; /* symmetry type of current piece */
int xx[36 * 36 * 2], yy[36 * 36 * 2], zz[36 * 36 * 2]; /* coordinates of current piece */
int xmin, xmax, ymin, ymax; /* range of coordinates */

```

8.  $\langle$  Generate the possible piece placements 8  $\rangle \equiv$

```
while ( $t$ ) {
    for ( $k = 1; k \leq 6; k++$ ) {
        if ( $k \leq s$ )  $\langle$  Output translates of the current piece 11  $\rangle$ ;
         $\langle$  Rotate the current piece 10  $\rangle$ ;
    }
     $\langle$  Transpose the current piece 9  $\rangle$ ;
     $t--$ ;
}
```

This code is used in section 6.

9.  $\langle$  Transpose the current piece 9  $\rangle \equiv$

```
for ( $j = 0; j < n; j++$ ) {
     $z = xx[j]$ ;
     $xx[j] = yy[j]$ ;
     $yy[j] = z$ ;
}
 $z = xmin; xmin = ymin; ymin = z$ ;
 $z = xmax; xmax = ymax; ymax = z$ ;
```

This code is used in section 8.

10.  $\langle$  Rotate the current piece 10  $\rangle \equiv$

```
 $xmin = ymin = 1000; xmax = ymax = -1000$ ;
for ( $j = 0; j < n; j++$ ) {
     $z = xx[j]$ ;
     $xx[j] = z + yy[j] + zz[j]$ ;
     $yy[j] = -z$ ;
     $zz[j] = 1 - zz[j]$ ;
    if ( $xx[j] < xmin$ )  $xmin = xx[j]$ ;
    if ( $xx[j] > xmax$ )  $xmax = xx[j]$ ;
    if ( $yy[j] < ymin$ )  $ymin = yy[j]$ ;
    if ( $yy[j] > ymax$ )  $ymax = yy[j]$ ;
}
```

This code is used in section 8.

11.  $\langle$  Output translates of the current piece 11  $\rangle \equiv$

```
for ( $x = bxmin - xmin; x \leq bxmax - xmax; x++$ )
    for ( $y = bymin - ymin; y \leq bymax - ymax; y++$ ) {
        for ( $j = 0; j < n; j++$ )
            if ( $\neg board[x + xx[j]][y + yy[j]][zz[j]]$ ) goto nope;
            printf(name);
        for ( $j = 0; j < n; j++$ ) {
            printf("\u25a1%c%c", encode( $x + xx[j]$ ), encode( $y + yy[j]$ ));
            if ( $zz[j]$ ) printf("*");
        }
        printf("\n");
    }
    nope: ;
}
```

This code is used in section 8.

12. ⟨ Subroutines 3 ⟩ +≡

```
char encode(x)
    int x;
{
    if (x < 10) return '0' + x;
    return 'a' - 10 + x;
}
```

**13. Index.**

*board*: 2, 4, 11.  
*buf*: 2, 4, 5, 6.  
*buf\_size*: 1, 2, 4, 5, 6.  
*bxmax*: 2, 4, 11.  
*bxmin*: 2, 4, 11.  
*bymax*: 2, 4, 11.  
*bymin*: 2, 4, 11.  
*c*: 3.  
*decode*: 2, 3, 6.  
*encode*: 11, 12.  
*exit*: 2.  
*fgets*: 2, 5, 6.  
*fprintf*: 2.  
*fwrite*: 2.  
*isspace*: 2, 6.  
*j*: 1.  
*k*: 1.  
*main*: 1.  
*max\_pieces*: 1.  
*n*: 1.  
*name*: 6, 7, 11.  
*nope*: 11.  
*p*: 1.  
*panic*: 2, 5, 6.  
*printf*: 5, 11.  
*q*: 1.  
*s*: 7.  
*stderr*: 2.  
*stdin*: 2, 5, 6.  
*stdout*: 2.  
*strlen*: 2, 6.  
*t*: 7.  
*x*: 1, 12.  
*xmax*: 6, 7, 9, 10, 11.  
*xmin*: 6, 7, 9, 10, 11.  
*xx*: 6, 7, 9, 10, 11.  
*y*: 1.  
*ymax*: 6, 7, 9, 10, 11.  
*ymin*: 6, 7, 9, 10, 11.  
*yy*: 6, 7, 9, 10, 11.  
*z*: 1.  
*zz*: 6, 7, 10, 11.

⟨ Generate the possible piece placements 8 ⟩ Used in section 6.  
⟨ Global variables 4, 7 ⟩ Used in section 1.  
⟨ Output translates of the current piece 11 ⟩ Used in section 8.  
⟨ Read and output the board 2 ⟩ Used in section 1.  
⟨ Read and output the piece names 5 ⟩ Used in section 1.  
⟨ Read and output the pieces 6 ⟩ Used in section 1.  
⟨ Rotate the current piece 10 ⟩ Used in section 8.  
⟨ Subroutines 3, 12 ⟩ Used in section 1.  
⟨ Transpose the current piece 9 ⟩ Used in section 8.

# POLYIAMONDS

	Section	Page
Data for dancing .....	<a href="#">1</a>	1
Index .....	<a href="#">13</a>	6